

## Doing Mathematics by Staring

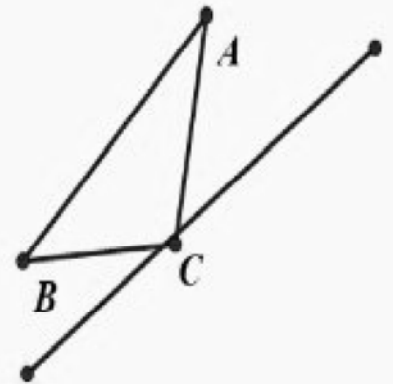
100AED AWARD

SOLVED. Winner I: Liana Hajeir (see Solution Below)

Imagine that you found yourself in a desert. You saw a line in sand and two holes A, B. (See Picture) You only have a very long piece of wood (Let say unmarked ruler). Using the unmarked ruler, you were able to find a point C on the line and you **constructed** the triangle ACB with minimum perimeter, i.e., if you choose a different point on the line, say d, then the perimeter of ADB  $\geq$  the perimeter of ACB.

How did you do that? state clearly the steps that you used in construction of such triangle.

Assume that you can draw line-segments or perpendicular line-segments just by using your finger and the unmarked ruler.





Winner : Liana Hajeir

- 1) We reflect B on  $l$ , and call the reflection D
- 2) This means that any point on  $l$  makes  $BC = DC$
- 3) Since the base AB is fixed, we want to minimize  $AC + BC$
- 4) Since  $BC = DC$ , we can say that we want to minimize  $AC + DC$
- 5) Since the shortest distance between 2 points is a straight line, we take C to be the point where  $l$  intersects with a straight line drawn from A to D ( $AC + DC$ )